

Sirindhorn International Institute of Technology
Thammasat University
Department of Common and Graduate Studies

MAS 116: Solution for Problem Set 6 (Part 2)

Semester/Year: 3/2008

Course Title: MAS116 (Mathematics I)

Instructor: Dr. Prapun Suksompong (prapun@siit.tu.ac.th)

Textbook: Howard Anton, Irl Bivens, and Stephen Davis, *Calculus*, 8th Edition, Wiley (2005).

Due date: Not Due

Section 6.1: 2, 8

Section 6.2: 1

Section 6.3: 1, 2, 5

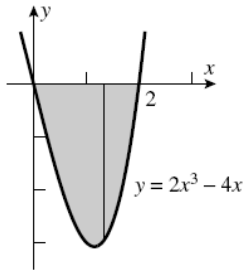
Section 10.5: 12, 14

Section 10.7: 8, 9, 20

Exercise Set 6.1

$$2. A = \int_0^4 (\sqrt{x} + x/4) dx = \left(2x^{3/2}/3 + x^2/8 \right) \Big|_0^4 = 22/3$$

$$8. A = \int_0^2 [0 - (x^3 - 4x)] dx \\ = \int_0^2 (4x - x^3) dx = 4$$



Exercise Set 6.2

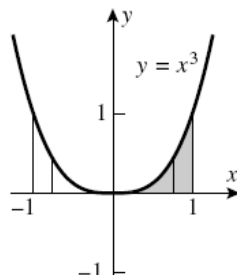
$$1. V = \pi \int_{-1}^3 (3 - x) dx = 8\pi$$

Exercise Set 6.3

$$1. V = \int_1^2 2\pi x(x^2) dx = 2\pi \int_1^2 x^3 dx = 15\pi/2$$

$$2. V = \int_0^{\sqrt{2}} 2\pi x(\sqrt{4-x^2} - x) dx = 2\pi \int_0^{\sqrt{2}} (x\sqrt{4-x^2} - x^2) dx = \frac{8\pi}{3}(2 - \sqrt{2})$$

$$\begin{aligned}
 5. \quad V &= \int_0^1 2\pi(x)(x^3)dx \\
 &= 2\pi \int_0^1 x^4 dx = 2\pi/5
 \end{aligned}$$



Exercise Set 10.5

$$12. \quad \rho = \lim_{k \rightarrow +\infty} \frac{4^{k+1}/(k+1)^2}{4^k/k^2} = \lim_{k \rightarrow +\infty} \frac{4k^2}{(k+1)^2} = 4, \text{ the series diverges}$$

$$14. \quad \rho = \lim_{k \rightarrow +\infty} \frac{(k+1)(1/2)^{k+1}}{k(1/2)^k} = \lim_{k \rightarrow +\infty} \frac{k+1}{2k} = 1/2, \text{ the series converges}$$

Exercise Set 10.7

$$8. \quad f^{(k)}(x) = a^k e^{ax}, \quad f^{(k)}(0) = a^k; \quad p_0(x) = 1, \quad p_1(x) = 1 + ax, \quad p_2(x) = 1 + ax + \frac{a^2}{2}x^2,$$

$$p_3(x) = 1 + ax + \frac{a^2}{2}x^2 + \frac{a^3}{3!}x^3, \quad p_4(x) = 1 + ax + \frac{a^2}{2}x^2 + \frac{a^3}{3!}x^3 + \frac{a^4}{4!}x^4; \quad \sum_{k=0}^n \frac{a^k}{k!}x^k$$

$$9. \quad f^{(k)}(0) = 0 \text{ if } k \text{ is odd, } f^{(k)}(0) \text{ is alternately } \pi^k \text{ and } -\pi^k \text{ if } k \text{ is even; } p_0(x) = 1, \quad p_1(x) = 1,$$

$$p_2(x) = 1 - \frac{\pi^2}{2!}x^2; \quad p_3(x) = 1 - \frac{\pi^2}{2!}x^2, \quad p_4(x) = 1 - \frac{\pi^2}{2!}x^2 + \frac{\pi^4}{4!}x^4; \quad \sum_{k=0}^{\lfloor \frac{n}{2} \rfloor} \frac{(-1)^k \pi^{2k}}{(2k)!}x^{2k}$$

NB: The function $\lfloor x \rfloor$ defined for real x indicates the greatest integer which is $\leq x$.

$$\begin{aligned}
20. \quad f^{(k)}(x) &= \frac{(-1)^k k!}{(x+2)^{k+1}}, \quad f^{(k)}(3) = \frac{(-1)^k k!}{5^{k+1}}; \quad p_0(x) = \frac{1}{5}; \quad p_1(x) = \frac{1}{5} - \frac{1}{25}(x-3); \\
p_2(x) &= \frac{1}{5} - \frac{1}{25}(x-3) + \frac{1}{125}(x-3)^2; \quad p_3(x) = \frac{1}{5} - \frac{1}{25}(x-3) + \frac{1}{125}(x-3)^2 - \frac{1}{625}(x-3)^3; \\
p_4(x) &= \frac{1}{5} - \frac{1}{25}(x-3) + \frac{1}{125}(x-3)^2 - \frac{1}{625}(x-3)^3 + \frac{1}{3125}(x-3)^4; \quad \sum_{k=0}^n \frac{(-1)^k}{5^{k+1}}(x-3)^k
\end{aligned}$$