

# ECS455 Formula Sheet

1D3	Limit: 40 symbols (or characters) per person.
012	$P_m = P_b = \frac{A^m}{m!} / \sum_{i=0}^{\infty} \frac{A^i}{i!}$ $A = \lambda \mu$ $E_{N_i} = \lambda T_i$
020	$P_N(x) = \begin{cases} \lambda s & , x=1 \\ 1-\lambda s & , x=0 \\ 0 & , \text{else} \end{cases}$
030	$B_{in} \sim N = \overset{\text{Ber}}{N_1 + \dots + N_n} = \sum_{k=1}^n N_k \xrightarrow{n \rightarrow \infty} \text{poiss}$
097	$B(n, p) \sim P_x(x) = \begin{cases} \binom{n}{x} p^x (1-p)^{n-x} & , x=0, \dots, n \\ 0 & , \text{else} \end{cases}$
123	
138	$\alpha = n p_1 = \lambda T$ $P(\alpha) \sim P_X(x) = \begin{cases} e^{-\alpha} \alpha^x / x! & , x=0 \\ 0 & , \text{else} \end{cases}$
161	$f_X(x) = \begin{cases} \lambda e^{-\lambda x} & , x > 0 \\ 0 & , x \leq 0 \end{cases}$
164	<p>Markov</p> $P[\text{1 new call}] = \lambda \delta$ $P[\text{1 call end}] = k \mu s$
171	$P[\text{1 new call}] = (n-k) \lambda \mu s$ $P[\text{1 call end}] = k \mu s$
172	$P_k = \frac{\binom{n}{k} A_u^k}{\sum_{i=0}^n \binom{n}{i} A_u^i}$
220	$\text{CDMA} \rightarrow S(t) = \sum_{k=0}^{2^L-1} s_k c_k(t)$
253	$g(x) = 1 + 0x + x^2 + x^3 \rightarrow \begin{matrix} 0 \rightarrow +1 \\ 1 \rightarrow -1 \\ \downarrow \uparrow \\ R_0 \quad R_1 \quad R_2 \end{matrix}$
272	$P_b = \frac{(n-m)/P_m}{\sum_{k=0}^n (n-k) P_k}$
339	$\text{Parseval} \int_{-\infty}^{\infty} x(t) y^*(t) dt = \int_{-\infty}^{\infty} X(f) Y^*(f) df$
363	$\langle a, b \rangle = \sum ab = 0$ $\langle a, b \rangle = \int_{-\infty}^{\infty} ab^* df = 0$ $\langle A, B \rangle = \int_{-\infty}^{\infty} ab^* df$ <p style="text-align: right;">} orthogonality</p>

387	$\text{TDMA} \rightarrow S(t) = \sum_{k=0}^{L-1} s_k p(t - kT_s) \quad \circ \overset{\uparrow}{\downarrow} \overset{\uparrow}{\downarrow} \circ$
388	$\hat{s}_k = \frac{1}{N} \langle y, c_k \rangle, \quad c_k^T = \frac{1}{N} c^T$ $\hat{s} = \frac{1}{N} r c^T$
401	$H_2 = \begin{bmatrix} 1 & 1 \\ 1 & -1 \end{bmatrix}, \quad H_N H_N^T = N I_N \rightarrow 2S$
427	$\text{FDMA} \rightarrow S(f) = \sum_{k=0}^{L-1} s_k P(f - k\Delta f)$
477	$\text{OFDM} S(t) = \sum_{k=0}^{N-1} s_k \frac{1}{\sqrt{N}} \int_{0, T_s}^{c_k(t)} \exp(j \frac{2\pi k t}{T_s})$
479	<p>Fading</p> $r(t) = x(t) * h(t) + n(t)$ $h(t) = \sum p_i \delta(t - \tau_i)$
483	$S_{DM} = S \left( n \frac{T_s}{N} \right) = \sqrt{N} \text{IDFT} \left\{ \frac{1}{\sqrt{N}} S_k \right\} [n]$ $\psi_N = e^{j 2\pi n / N} \rightarrow 3 \text{ S}$
486	$\psi_N = e^{j \frac{2\pi n}{N}}, \quad \Psi_N = \begin{bmatrix} 1 & \psi_N^{-1} & \dots & \psi_N^{-(N-1)} \\ \vdots & \psi_N^{-1} & \dots & \psi_N^{-(N-1)} \\ \vdots & \psi_N^{-1} & \dots & \psi_N^{-(N-1)} \\ \vdots & \psi_N^{-1} & \dots & \psi_N^{-(N-1)} \end{bmatrix}$
577	$\psi_N^{-1} = \frac{1}{N} \psi_N^*, \quad x = \frac{1}{N} \psi_N^* X \Leftrightarrow X = \psi_N x$
658	$S^{(L)} [n] = S \left( n \frac{T_s}{L N} \right) = \sqrt{LN} \text{IDFT} \left\{ S_k \right\} [n]$
709	$\hat{S}_k = \begin{cases} s_k, & 0 \leq k < N \\ 0, & N \leq k \leq LN \end{cases}$
867	$\{x * h\} [n] = \sum_m x[m] h[n-m]$
892	$[1 \ 2 \ 3 \ 0 \ 0] \otimes [4 \ 5 \ 6 \ 0 \ 0] = [1 \ 2 \ 3] * [4 \ 5 \ 6]$
950	$[1 \ -2 \ 0 \ 1 \ 2] \oplus [3 \ 2 \ 1 \ 0 \ 0] =$ $[1 \ 2 \ 1 \ -2 \ 3 \ 1 \ 2] * [3 \ 2 \ 1] \text{ w/ junk}$