## Solution ECS 452: In-Class Exercise # 2

## **Instructions**

- 1. Separate into groups of no more than three persons.
- 2. The group cannot be the same as your former group.
- 3. Only one submission is needed for each group.
- 4. Write down all the steps that you have done to obtain your answers. You may not get full credit even when your answer is correct without showing how you get your answer.
- 5. Do not panic.

Date: 0_2 / 0_2 / 2017					
Name		ID (last 3 digits)			
Prapun	5	5	5	5	

1. Write each of the following quantities in the form X.XXX (possibly with the help of your calculator).

a. 
$$-\log_2(1/16) = -\log_2(\frac{1}{8}) = -\log_2 2^{-3} = -(-3) = 3 \approx 3.600$$

c. 
$$-(0.3)\log_2(0.3) - (0.7)\log_2(0.7) \approx 0.8813$$

0.5211
2. Consider a random variable X having four possible values. Their probabilities are

Find the entropy (per symbol) of this random variable.

$$H(P) = H(X) = -\frac{2}{5} p_{X}(x)^{\log_{2} p_{X}(x)}$$

$$= -\frac{1}{6} \log_{2} \frac{1}{6} - \frac{2}{9} \log_{2} \frac{2}{9} - \frac{5}{15} \log_{2} \frac{5}{15} - \frac{1}{3} \log_{2} \frac{1}{3}$$

$$\approx 0.4308 + 0.4822 + 0.5133 + 0.5283 \approx 1.9547$$

3. Consider a random variable X having four possible values. Their probabilities are

Find the **entropy** (per symbol) of this random variable.

$$H(x) = -\frac{2}{x} P_{x}(x) \log_{2} P_{x}(x)$$

$$= -\frac{3}{24} \log_{2} \frac{3}{24} - \frac{5}{24} \log_{2} \frac{5}{24} - \frac{7}{24} \log_{2} \frac{7}{24} - \frac{9}{24} \log_{2} \frac{9}{24}$$

$$\approx 0.3750 + 0.4715 + 0.5185 + 0.5306 = 1.8956$$