

NAME 9

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ECS 452: Digital Communication Systems

2015/2

HW 6 — Due: Apr 20

Lecturer: Asst. Prof. Dr. Prapun Suksompong

Instructions

- (a) Solve all non-optional problems. (5 pt)
 - (i) Write your first name and the last three digit of your student ID on the upper-right corner of *every* submitted page.
 - (ii) For each part, write your explanation/derivation and answer in the space provided.
- (b) ONE part of a question will be graded (5 pt). Of course, you do not know which part will be selected; so you should work on all of them.
- (c) Late submission will be rejected.
- (d) **Write down all the steps** that you have done to obtain your answers. You may not get full credit even when your answer is correct without showing how you get your answer.

Problem 1. Consider a block code whose generator matrix is

$$\mathbf{G} = \begin{bmatrix} 1 & 0 & 0 & 1 & 0 & 1 \\ 0 & 1 & 0 & 0 & 1 & 1 \\ 0 & 0 & 1 & 1 & 1 & 0 \end{bmatrix}$$

- (a) Suppose the message is $\mathbf{b} = [101]$. Find the corresponding codeword \mathbf{x} .

$$\mathbf{x} = \mathbf{bG} = [101] \left[\begin{array}{ccc|ccc} 1 & 0 & 0 & 1 & 0 & 1 \\ 0 & 1 & 0 & 0 & 1 & 1 \\ 0 & 0 & 1 & 1 & 1 & 0 \end{array} \right] = [101011]$$

- (b) In the provided table, list all possible data (message) vectors \mathbf{b} in the left column (one in each row). Then, find the corresponding codewords \mathbf{x} and their weights in the second and third columns, respectively.