Instructions

- 1. Separate into groups of no more than three persons.
- 2. The group cannot be the same as your former group.
- 3. Only one submission is needed for each group.
- Write down all the steps that you have done to obtain your answers. You
 may not get full credit even when your answer is correct without showing
 how you get your answer.

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Name	ID
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1. Consider a DMC whose
$$\mathcal{X} = \{1, 2, 3\}$$
, $\mathcal{Y} = \{1, 2, 3, 4\}$, and $\mathbf{Q} = \begin{bmatrix} 0.2 & 0.6 & 0.1 & 0.1 \\ 0.1 & 0.7 & 0.1 & 0.1 \\ 0.3 & 0.3 & 0.3 & 0.1 \end{bmatrix}$.

Suppose the prior probability vector is $\mathbf{p} = \begin{bmatrix} 0.2 & 0.1 & 0.7 \end{bmatrix}$.

a. Find the joint pmf matrix **P**.

b. Find the MAP detector and its error probability.

For each column of the P matrix, select the max value.

The corresponding x-value for the selected value in each column.

P(C) = 0.21+0.21+0.21+0.07 = 0.7

So,
$$\hat{x}_{MAP}(y) \equiv 3$$
.

P(E) = 1-P(C) = 1-0.7 = 0.3

c. Find the ML detector and its error probability.

