## ECS 332: In-Class Exercise # 9 - Sol

## Instructions

- 1. Separate into groups of no more than three students each. The group cannot be the same as any of your former groups.
- Explanation is not required for this exercise [ENRE]
- 3. **Do not panic.**

| Date: <u>19/09</u> /2019 |    |                    |   |
|--------------------------|----|--------------------|---|
| Name                     | II | ID (last 3 digits) |   |
| Prapun                   | 5  | 5                  | 5 |
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|                          |    |                    |   |

1. For each of the following signal g(t), find its (normalized) average power  $P_g \equiv \langle |g(t)|^2 \rangle$ .

| Do not use any approximation.                              | $g(t) \qquad P_g = \langle  g(t) ^2 \rangle$   |  |  |
|--|--|--|--|
| g(t)   | Linear combination of<br>complex exponential<br>functions<br>[4.23] $\sum_{k} c_k e^{j2\pi f_k t}$<br>where the $f_k$ are distinct $\sum_{k}  c_k ^2$  |  |  |
| $g(t) = 10e^{j20\pi t}$                                    | Linear combination of sinusoids<br>[4.28] $\sum_{k} A_k \cos(2\pi f_k t + \phi_k)$ where the $f_k$ are positive and distinct $\frac{1}{2} \sum_{k}  A_k ^2$ $P_g = 10^2 = 100.$  |  |  |
| $g(t) = 10e^{j20\pi t} + 5e^{j40\pi t}$                    | First, we check that the freq. of the two terms are different<br>which is the case here. Therefore,<br>$P_g = 10^2 + 5^2 = 125$ .  |  |  |
| $g(t) = \left(10e^{j20\pi t} + 5e^{j40\pi t}\right)^2$     | $g(t) = (10e^{j20\pi t})^{2} + 2(10e^{j20\pi t})(5e^{j40\pi t}) + (5e^{j40\pi t})^{2}$<br>= 100e^{j40\pi t} + 100e^{j60\pi t} + 25e^{j80\pi t}.<br>These terms have different freq. Therefore,<br>$P_{g} = 100^{2} + 100^{2} + 25^{2} = 20625.$  |  |  |
| $g(t) = 4\cos(4t + 4^\circ)$                               | For sinusoidal signals, don't forget that we have an additional factor of $\frac{1}{2}$ .<br>$P_g = \frac{1}{2} \times 4^2 = 8.$   |  |  |
| $g(t) = 5\cos(3t+15^\circ) + 12\cos(4t+105^\circ)$         | First, we check that the freq. of the two terms are different<br>and positive which is the case here. Therefore,<br>$P_g = \frac{1}{2} \times 5^2 + \frac{1}{2} \times 12^2 = 84.5.$   |  |  |
| $g(t) = 5\cos(3t + 15^{\circ}) + 12\cos(3t + 105^{\circ})$ | The freq. of the two terms are the same. Therefore, we must<br>combine them first:<br>$g(t) \Leftrightarrow 5 \angle 15^\circ + 12 \angle 105^\circ = 13 \pounds 82.38^\circ$<br>$\Leftrightarrow 13\cos(3t + 82.38^\circ).$<br>Therefore, $P_g = \frac{1}{2} \times 13^2 = 84.5.$<br>Note that we don't need this ang |  |  |

We only need the magnitude for our power calculation. Knowing that the angle difference

between the two terms is 90°, we can use Pythagoras' theorem:  $\sqrt{5^2 + 12^2} = 13$ .