

HW 9 — Due: Not Due

Lecturer: Prapun Suksompong, Ph.D.

Problem 1. State the Nyquist's (first) criterion for zero ISI

- (a) In the time domain.
- (b) In the frequency domain.

Problem 2. In each part below, a pulse $P(f)$ is defined in the frequency domain from $f = 0$ to $f = 1$. Outside of $[0, 1]$, your task is to assign value(s) to $P(f)$ so that it becomes a Nyquist pulse. Of course, you will also need to specify the symbol interval T as well.

Hint: To avoid dealing with complex-valued $P(f)$, you may assume that $p(t)$ is real-valued and even; in which case $P(f)$ is also real-valued and even.

- (a) Find a Nyquist pulse $P(f)$ whose $P(f) = 0.5$ on $[0, 1]$.
- (b) Find a Nyquist pulse $P(f)$ whose $P(f) = 0.25$ on $[0, 1]$.
- (c) Find a Nyquist pulse $P(f)$ whose

$$P(f) = \begin{cases} 0.5, & 0 \leq f < 0.5 \\ 0.25, & 0.5 \leq f \leq 1 \end{cases}$$

- (d) Find a Nyquist pulse $P(f)$ whose

$$P(f) = \begin{cases} 0.5, & f \in [0, 0.25) \cup [0.5, 0.75) \\ 0.25, & f \in [0.25, 0.5) \cup [0.75, 1] \end{cases}$$

Problem 3. Consider a raised cosine pulse $p_{\text{RC}}(t; \alpha)$ and its Fourier transform $P_{\text{RC}}(f; \alpha)$. Assume the rolloff factor $\alpha = 0.3$ and the symbol "duration" $T = 1$.

- (a) Carefully sketch $P_{\text{RC}}(f; \alpha)$.
- (b) Find $p_{\text{RC}}(2; \alpha)$.
- (c) Find $P_{\text{RC}}(0.5; \alpha)$.
- (d) Find $P_{\text{RC}}(0.3; \alpha)$.

- (e) *Find $P_{RC}(0.4; \alpha)$.

Remark: You should be able to solve this problem without referring to the “ugly” expression(s).

Problem 4. Consider a raised cosine pulse $p(t)$ with rolloff factor α and symbol “duration” T .

- (a) Find $p(T/2)$ as a function of α .
- (b) Use `MATLAB` to plot $p(T/2)$ as a function of α .