

ECS 315: Probability and Random Processes

2019/1

HW 1 — Due: August 29, 4 PM

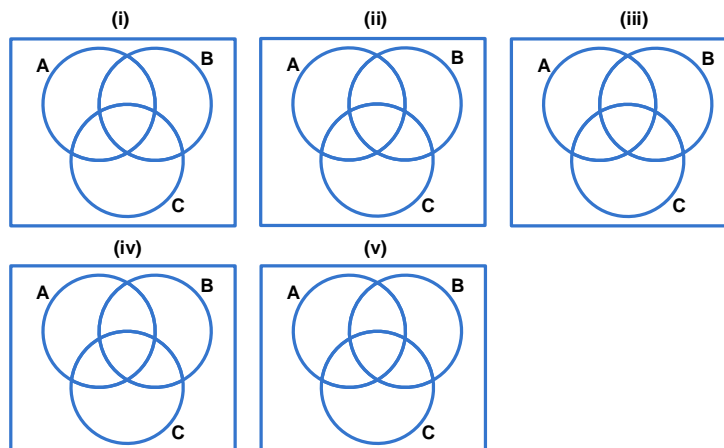
Lecturer: Prapun Suksompong, Ph.D.

Instructions

- (a) This assignment has 2 pages.
- (b) (1 pt) Work and write your answers **directly on this sheet** (not on another blank sheet of paper). Hard-copies are distributed in class.
- (c) (1 pt) Write your first name and the last three digits of your student ID in the spaces provided on the upper-right corner of this page.
- (d) (8 pt) Try to solve all problems.
- (e) [ENRpr] = Explanation is not required for this problem.
- (f) Late submission will be heavily penalized.

Problem 1. (Set Theory) [ENRpr]

- (a) In the Venn diagrams below,



shade the region that corresponds to the following events:

- (i) A^c
- (ii) $A \cap B$
- (iii) $(A \cap B) \cup C$
- (iv) $(B \cup C)^c$
- (v) $(A \cap B)^c \cup C$

[Montgomery and Runger, 2010, Q2-19]

- (b) Let $\Omega = \{0, 1, 2, 3, 4, 5, 6, 7\}$, and put $A = \{1, 2, 3, 4\}$, $B = \{3, 4, 5, 6\}$, and $C = \{5, 6\}$. Find

- (i) $A \cup B$
- (ii) $A \cap B$
- (iii) $A \cap C$
- (iv) A^c
- (v) $B \setminus A$

Problem 2. [ENRpr] For each of the sets provided in the first column of the table below, indicate (by putting a Y(es) or an N(o) in the appropriate cells of the table) whether it is “finite”, “infinite”, “countable”, “countably infinite”, “uncountable”.

Sets	Finite	Infinite	Countable	Countably Infinite	Uncountable
$\{1\}$					
$\{1, 2\}$					
$[1, 2]$					
$[1, 2] \cup [-1, 0]$					
$\{1, 2, 3, 4\}$					
the power set of $\{1, 2, 3, 4\}$					
the set of all real numbers					
the set of all real-valued x satisfying $\cos x = 0$					
the set of all integers					
$(-\infty, 0]$					
$(-\infty, 0] \cap [0, +\infty)$					