Textbook: [Y\&G] R. D. Yates and D. J. Goodman, Probability and Stochastic Processes: A Friendly Introduction for Electrical and Computer Engineers, 2nd ed., Wiley, 2004. Call No. QA273 Y384 2005.

| Topics | [Y\&G] |
| :---: | :---: |
| 1. Probability and You |  |
| a. Randomness |  |
| b. Background on Some Frequently Used Examples |  |
| i. Coins |  |
| ii. Dice |  |
| iii. Cards |  |
| c. A Glimpse at Probability Theory |  |
| i. Random experiment | p. 7-8 |
| ii. Outcomes and Sample space | p. 8 |
| iii. Event | p. 8-9 |
| iv. Relative Frequency | p. 12-13, 67 |
| v. Law of Large Numbers | p. 12-13, 67 |
| vi. Using MATLAB to generate and analyze the sequence of coin flipping | p. 40 <br> [Y\&G] uses the rand and hist commands. |
| 2. Review of Set Theory | Section 1.1 Set Theory |
| a. Venn diagram, basic set operations/identities (e.g. de Morgan Laws) | p. 2 |
| b. Disjoint sets | p. 5 |
| c. Partition | p. 10-11 <br> (This is called event space in [Y\&G]) |
| d. Cardinality, Finite set, Countable Sets, Countably Infinite Sets, Uncountable Sets, Singleton |  |
| i. Useful for checking whether a random variable is discrete or continuous |  |
| e. Terminology of set theory and probability. | p. 9 |
| 3. Classical Probability |  |
| a. Assumptions |  |
| b. Basic properties |  |
| 4. Enumeration / Combinatorics / Counting | Section 1.8 Counting Methods |
| a. Four Principles |  |
| i. Addition |  |
| ii. Multiplication | p. 28 |
| iii. Subtraction |  |
| iv. Division |  |
| b. Four Kinds of Counting Problems |  |
| i. Ordered sampling with replacement | p. 31-32 |
| ii. Ordered sampling without replacement ( $r$-permutation) | p. 29 |
| 1. Factorial and permutation | p. 29 |


| 2. Permutations with types and multinomial coefficient | p. 33-34 |
| :---: | :---: |
| iii. Unordered sampling of without replacement (r-combinations) | p. 29-31 <br> [Y\&G] also defines the formula for $r$ that is not between 0 and $n$. |
| iv. Unordered sampling with replacement |  |
| 1. bars and stars argument |  |
| c. Binomial Theorem and Multinomial Theorem |  |
| d. Famous Example: Galileo and the Duke of Tuscany |  |
| e. Application: Success Runs |  |
| 5. Probability Foundations | Section 1.3 Probability Axioms Section 1.4 Some Consequences of the Axioms |
| a. Kolmogorov's Axioms for Probability | p. 12 <br> In [Y\&G], the probability measure P() is represented by $\mathrm{P}[$ ]. |
| b. Consequences of Axioms | p. 13, 15-16 <br> Note that in [Y\&G] with is pointed out that we can write $\mathrm{P}[\mathrm{AB}]$ or $\mathrm{P}[\mathrm{A}, \mathrm{B}]$ to represent $\mathrm{P}[\mathrm{A} \cap \mathrm{B}]$ |
| c. Connection to classical probability | p. 14 |
| 6. Event-based Independence and Conditional Probability |  |
| a. Event-based Conditional Probability | Section 1.5 Conditional Probability p. 16-21 |
| i. Tree diagram | Section 1.7 Sequential Experiments and Tree Diagrams <br> p. 24-28 |
| 1. Compact form |  |
| b. Event-based Independence | Section 1.6 Independence <br> p. 21-24 |
| c. Bernoulli Trials | Section 1.9 Independent Trials p. 35-36 |

