

ECS 315: In-Class Exercise #11 Solution

Instructions

1. Separate into groups of no more than three persons. Only one submission is needed for each group. **The group cannot be the same as any of your former groups.**
2. **Write down all the steps** that you have done to obtain your answers. You may not get full credit even when your answer is correct without showing how you get your answer.
3. **Do not panic.**

Date: **16** / **11** / 2017

Name

ID (last 3 digits)

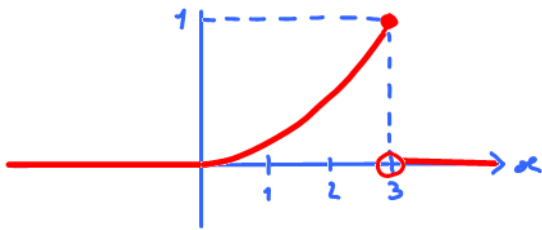
Prapun

5	5	5

Consider a continuous random variable whose pdf is given by $f_X(x) = \begin{cases} \frac{1}{9}x^2, & x \in [0, 3], \\ 0, & \text{otherwise.} \end{cases}$

a) Plot $f_X(x)$

$$f_X(3) = \frac{1}{9} \times 3^2 = 1$$



b) Find $P[1 < X < 2]$

$$P[1 < X < 2] = \int_1^2 f_X(x) dx = \int_1^2 \frac{1}{9}x^2 dx = \left. \frac{1}{9} \frac{x^3}{3} \right|_1^2 = \frac{8-1}{27} = \frac{7}{27}$$

c) Find $P[X < 1]$

$$\begin{aligned} P[X < 1] &= P[-\infty < X < 1] = \int_{-\infty}^1 f_X(x) dx = \int_{-\infty}^0 \underbrace{f_X(x)}_{=0} dx + \int_0^1 f_X(x) dx \\ &= 0 + \int_0^1 \frac{1}{9}x^2 dx = \left. \frac{1}{27}x^3 \right|_0^1 = \frac{1}{27} \end{aligned}$$

d) Find $P[X > 4]$

$$P[X > 4] = P[4 < X < \infty] = \int_4^{\infty} f_X(x) dx = \int_4^{\infty} 0 dx = 0$$