

HW9: Questions from [Yates & Goodman, 2005]

Q4.4.2

Random variables X and Y have joint PDF

$$f_{X,Y}(x, y) = \begin{cases} cxy^2 & 0 \leq x \leq 1, 0 \leq y \leq 1, \\ 0 & \text{otherwise.} \end{cases}$$

(a) Find the constant c .

(b) Find $P[X > Y]$ and $P[Y < X^2]$.

Q4.4.3

Random variables X and Y have joint PDF

$$f_{X,Y}(x, y) = \begin{cases} 6e^{-(2x+3y)} & x \geq 0, y \geq 0, \\ 0 & \text{otherwise.} \end{cases}$$

(a) Find $P[X > Y]$ and $P[X + Y \leq 1]$.

Q4.6.8

Random variables X and Y have joint PDF

$$f_{X,Y}(x, y) = \begin{cases} 2 & 0 \leq y \leq x \leq 1, \\ 0 & \text{otherwise.} \end{cases}$$

Let $W = Y/X$.

(a) What is S_W , the range of W ?

(b) Find $F_W(w)$, $f_W(w)$, and $E[W]$.

Q4.7.8

Random variables X and Y have joint PDF

$$f_{X,Y}(x, y) = \begin{cases} (x + y)/3 & 0 \leq x \leq 1; \\ & 0 \leq y \leq 2, \\ 0 & \text{otherwise.} \end{cases}$$

- (a) What are $E[X]$ and $\text{Var}[X]$?
- (b) What are $E[Y]$ and $\text{Var}[Y]$?
- (c) What is $\text{Cov}[X, Y]$?
- (d) What is $E[X + Y]$?
- (e) What is $\text{Var}[X + Y]$?

Q4.7.12

Random variables X and Y have joint PDF

$$f_{X,Y}(x, y) = \begin{cases} 1/2 & -1 \leq x \leq y \leq 1, \\ 0 & \text{otherwise.} \end{cases}$$

Find $E[XY]$ and $E[e^{X+Y}]$.

Q4.11.1

Random variables X and Y have joint PDF

$$f_{X,Y}(x, y) = ce^{-(x^2/8)-(y^2/18)}.$$

What is the constant c ? Are X and Y independent?