ECS 315: In-Class Exercise # 18

Instructions

 Separate into groups of no more than three students each. The group cannot be the same as any of your former groups after the midterm.

Write down all the steps that you have done to obtain your answers. You may not get full credit even when your answer is correct without showing how you get your answer.

3. **Do not panic.**

Date: <u>29/10</u> /2019			
Name	ID	(last 3 d	igits)
Prapun	5	5	5

1. Find $\mathbb{E}[X^2]$ and Var[X] for the random variable X defined in each part below:

$p_{X}(x)$	$\mathbb{E}[X]$	$\mathbb{E}ig[X^2ig]$	Var[X]
$\begin{cases} \frac{1}{3}x, & x \in \{1, 2\}, \\ 0, & \text{otherwise.} \end{cases}$	<u>5</u> 3	$= \sum_{x} x^{2} p_{X}(x)$ $= (1^{2} \times p_{X}(1)) + (2^{2} \times p_{X}(2))$ $= (1 \times \frac{1}{3}) + (4 \times \frac{2}{3}) = \frac{9}{3} = 3.$	$= \mathbb{E}[X^2] - (\mathbb{E}X)^2$ $= \frac{9}{3} - \left(\frac{5}{3}\right)^2 = \frac{2}{9}$
$\begin{cases} 0.3, & x = -1, 1, \\ 0.4, & x = 3, \\ 0, & \text{otherwise.} \end{cases}$	1.2	$= \sum_{x} x^{2} p_{X}(x)$ $= ((-1)^{2} \times p_{X}(-1)) + (1^{2} \times p_{X}(1)) + (3^{2} \times p_{X}(3))$ $= (1 \times 0.3) + (1 \times 0.3) + (9 \times 0.4)$ $= 4.2 = \frac{21}{5}$	$= \mathbb{E}[X^2] - (\mathbb{E}X)^2$ $= 4.2 - (1.2)^2$ $= 2.76 = \frac{69}{25}$
$\begin{cases} \frac{1}{55}x, & x \in \{1, 2, 3,, 10\}, \\ 0, & \text{otherwise.} \end{cases}$	7	$= \sum_{x} x^{2} p_{X}(x) = \sum_{x=1}^{10} x^{2} \left(\frac{1}{55}x\right)$ $= \frac{1}{55} \sum_{x=1}^{10} x^{3} = \frac{55^{2}}{55} = 55$ Note that $\sum_{x=1}^{n} x^{3} = 1^{3} + 2^{3} + 3^{3} + \dots + n^{3}$ $= \left[\frac{n(n+1)}{2}\right]^{2}$	$= \mathbb{E}[X^2] - (\mathbb{E}X)^2 = 55 - (7)^2 = 6$