## Sirindhorn International Institute of Technology Thammasat University at Rangsit

School of Information, Computer and Communication Technology

| COURSE | $:$ ECS 204 Basic Electrical Engineering Lab |
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| EXPERIMENT | $: 08$ Operational Amplifiers II |

## I. OBJECTIVE

To study the use of operational amplifier in converters and integrator.

## II. BASIC INFORMATION

## II. 1 Op-Amp 741

1. The pin details of op amp 741 are shown in Figure 1 below.


Figure 1: Pin details and configuration of IC 741.

Caution: An op-amp must be treated with special care. They are powerful but can be easily damaged from wrong circuit wiring. In particular it is abusive to apply AC-signal voltages to the input terminals before providing the power supply (or fully powering up the device), or to exceed certain maximum limits. Therefore, for each section of this experiment, follow the following steps.
i. Set up the circuit with all signal sources turned off.
ii. Double-check your connection.
iii. Enable the power supply (i.e. power up the op amp device).
iv. Turn up the signal source.
v. Op amps can also be damaged if their outputs are shorted to ground or to the power supply. Please also be very careful with wiring.
2. Two important characteristics of the ideal op amp are

1) The currents into both input terminals are zero:

$$
i_{+}=i_{-}=0 .
$$

2) The voltage across the input terminals is negligibly small:

$$
v_{+} \approx v_{-} .
$$

Remark: Do not assume that $v_{+}=v_{-}=0$ !


## II. 2 Voltage-to-Current Converter and Current-to-Voltage Converter

1. The voltage-to-current and current-to-voltage converters are used in electronic voltmeters and ammeters, respectively.
2. The voltage-to-current converter, as shown in Figure 2, produces an output current that depends on the input voltage and the resistor R. In particular, the output current is given by

$$
\mathrm{I}_{\text {out }}=\mathrm{V}_{\mathrm{i}} / \mathrm{R}
$$

independent of the loading resistance $\mathrm{R}_{\mathrm{L}}$.
3. The current-to-voltage converter, as shown in Figure 3, produces an output voltage that depends on the input current and the resistor R . In particular, the output voltage is given by

$$
\mathrm{V}_{\mathrm{o}}=-\mathrm{I}_{\mathrm{in}} \mathrm{R}
$$

independent of the loading resistance $\mathrm{R}_{\mathrm{L}}$.


Figure 2: Voltage-to-current converter.


Figure 3: Current-to-voltage converter.

## II. 3 Inverting Integrator

1. An inverting integrator is shown in Figure 4.


Figure 4: Inverting Integrator

Since no current enters the inverting input of an ideal op amp, all input currents must flow through the capacitor. Thus, $\mathrm{i}_{\mathrm{c}}=\mathrm{i}_{\mathrm{in}}$. Moreover, for ideal op amp, we know that the voltage at the two input terminals must be the same. Therefore, $\mathrm{v}_{\mathrm{X}}=0$. This gives $\mathrm{i}_{\mathrm{in}}=$ $v_{i} /$ R. Recall the relationship between the time-dependent current and voltage for the capacitor:

$$
i_{C}(t)=C \frac{d}{d t} v_{C}(t)
$$

In this case, the current through the capacitor is

$$
i_{C}(t)=i_{\mathrm{in}}(t)=\frac{v_{i}(t)}{R}
$$

and the voltage across the capacitor is

$$
v_{C}(t)=v_{X}-v_{o}(t)=-v_{o}(t) .
$$

Hence,

$$
\frac{v_{i}(t)}{R}=-C \frac{d}{d t} v_{o}(t) .
$$

The output voltage then has the following form:

$$
v_{o}(t)=v_{o}(0)-\frac{1}{R C} \int_{0}^{t} v_{i}(\tau) d \tau,
$$

where $v_{o}(0)$ is the initial value of the output voltage. Note that the change in the output voltage (when considered at two time instants $t_{1}$ and $t_{2}$ ) is inversely proportional to the integration of the input voltage.

$$
v_{o}\left(t_{2}\right)-v_{o}\left(t_{1}\right)=-\frac{1}{R C} \int_{t_{1}}^{t_{2}} v_{i}(t) d t
$$

Suppose the input voltage waveform $v_{i}$ is a square wave with frequency $f$ and peak-topeak voltage $2 h$ as shown in Figure 5a.

(a) Input waveform

(b) Output waveform

Figure 5: Input and corresponding output waveform to the integrating amplifier in Figure 4.

For half of the period, the input is fixed at $+h$. During this time, the output will decrease. At the end of this interval, the total decrease is

$$
\frac{1}{R C} h \times \frac{T}{2}=\frac{h}{2 f R C} .
$$

Similarly, the output will increase during the time that the input is fixed at $-h$. Because input has equal areas above and below the ground level, the decrease amount is the same as the increase amount and we see a triangular waveform at the output. The peak-to-peak
voltage is $h /(2 f R C)$ as shown in Figure 5b. In conclusion, when a square wave drives an op amp integrator, the output is a triangular wave.
Remark: For the circuit in Figure 4, an input with nonzero mean (DC offset) can saturate the op amp. To see this, suppose the range of the square wave input is from -1 to 2 V . Then, during each period of the input, the output will have a $\frac{2}{2 f R C}$ decrease and a $\frac{1}{2 f R C}$ increase.

Because the amount of decrease is greater, the output will accumulate this difference during each period. It will keep decreasing until it saturates the op amp.
2. The analysis provided earlier is performed in time domain. Alternatively, we can analyze the integrator in Figure 4 in frequency domain via steady-state AC analysis. In particular, suppose the input is sinusoidal with peak $V_{i}$ and frequency $f$.
In AC analysis, we use impedance. The relationship between the current and voltage for the capacitor is

$$
V_{C}=I_{C} \times Z_{C}=I_{C} \times \frac{1}{j \omega C} .
$$

For ideal op amp, we again have

$$
I_{C}=I_{\mathrm{in}}=\frac{V_{i}}{R}
$$

and

$$
V_{C}=V_{X}-V_{o}=-V_{o} .
$$

Hence,

$$
V_{o}=-V_{C}=-I_{C} \times \frac{1}{j \omega C}=-\left(\frac{V_{i}}{R}\right) \times \frac{1}{j \omega C} .
$$

Therefore, the gain at frequency $f$ is

$$
-\frac{1}{j 2 \pi f R C} .
$$

In particular, the gain at $f=0$ is unbounded.
Recall, from your calculus class, that you can decompose a periodic waveform into a sum of weighted sinusoidal waveforms. If your waveform has a nonzero average, then you have a constant in your sum as well. This constant is the DC offset. Our frequencydomain analysis above shows that if the DC offset is nonzero, it will be (theoretically) amplified by an infinite gain! This will saturate the op amp.
3. In practical circuit, a resistor $\mathrm{R}_{\mathrm{p}}$ is usually shunted across the capacitor as shown in Figure 6. In this case,

$$
V_{C}=I_{\mathrm{in}} \times\left(Z_{C} / / R_{p}\right)=\frac{V_{i}}{R} \frac{1}{j \omega C+\frac{1}{R_{p}}}=\frac{V_{i}}{R} \frac{R_{p}}{j \omega R_{p} C+1} .
$$

So,

$$
V_{o}=-V_{C}=-\frac{V_{i}}{R} \frac{R_{p}}{j \omega R_{p} C+1}
$$

and the gain is

$$
\frac{V_{o}}{V_{i}}=-\frac{1}{R} \frac{R_{p}}{j \omega R_{p} C+1} .
$$

With the added $\mathrm{R}_{\mathrm{p}}$, at $f=0$, the gain is finite.


Figure 6: Inverting Integrator with shunt resistor

Large $R_{p}$ is used so that the overall operation of the circuit is not too different from the original integrating amplifier.

One important effect of adding $R_{p}$ is that the output will not be triangular anymore. You will still observe an output that is very similar to a triangular waveform if the product $R_{p} C$ is large compared to the half-period time $\mathrm{T} / 2$.

It can be shown that if the input is a zero-mean square wave with frequency $f$ and peak-to-peak voltage $2 h$ then, the output will be zero-mean waveform with peak-to-peak voltage

$$
2 h \frac{R p}{R} \frac{1-r}{1+r},
$$

where $r=\exp \left(-\frac{1}{2 f R_{p} C}\right)$.

## III. MATERIALS REQUIRED

Power supplies:
$\pm 12 \mathrm{~V}, \mathrm{DC}$, regulated
Variable 0-15 V
Equipment:
Oscilloscope
Function generator
Multi-meter
Resistors:
two $1-\mathrm{k} \Omega$
one $100-\mathrm{k} \Omega$
one $12-\mathrm{k} \Omega$
Semiconductor:
one op amp 741
Capacitors:
one $0.001 \mu \mathrm{~F} \quad$ one $0.01 \mu \mathrm{~F} \quad$ one $0.047 \mu \mathrm{~F}$

## IV PROCEDIRE

## Part A: Voltage-to-current converter

1. Connect the circuit of Figure 7.

Remark:
(1) Recall how to generate the +12 V and -12 V from the previous experiment.
(2) Do not forget to put all the grounds at the same node.
2. Adjust voltage supply $\mathrm{V}_{\text {in }}$ according to the value listed in Table 8-1.

Record the corresponding $I_{\text {out }}$.


Figure 7: Voltage-to-current converter.

## Part B: Current-to-voltage converter

1. Connect the circuit of Figure 8.
2. Adjust the voltage supply $\mathrm{V}_{\text {in }}$ such that the current $\mathrm{i}_{\text {in }}$ according to Table 8-2 is obtained.
3. Measure $\mathrm{V}_{\text {out }}$ and record the result in Table 8-2.


Figure 8: Current-to-voltage converter.

Caution: Do not connect the output directly to the ground.

## Part C: Op amp Integrator

1. Connect the circuit shown in Figure 9.
2. Observe $v_{i n}(t)$ and $v_{\text {out }}(t)$ of the circuit for several values of $C$ and record the results as prescribed in Table 8-3.
Note that you can use different volts/div for $v_{\text {in }}$ and $v_{\text {out }}$.


Figure 9: Op amp integrator.

TABLE 8-1: Voltage-to-current converter
$\mathrm{R}=$ $\qquad$

| $\mathrm{V}_{\text {in }}, \mathrm{V}$ |  | $\mathrm{I}_{\text {out }}, \mathrm{mA}$ |
| :---: | :---: | :---: |
| 1 |  |  |
| 3 |  |  |
| 6 |  |  |
| 10 |  |  |

TA's Signature: $\qquad$
TABLE 8-2: Current-to-voltage converter
$\mathrm{R}=$ $\qquad$

| $\mathrm{I}_{\text {in }}, \mathrm{mA}$ |  | $\mathrm{V}_{\text {out, }, \mathrm{V}}$ |
| :---: | :---: | :---: |
| 1 |  |  |
| 3 |  |  |
| 6 |  |  |
| 10 |  |  |

TA's Signature: $\qquad$

TABLE 8-3: Op amp integrator

| $\mathrm{C}=0.047 \mu \mathrm{~F}$ | Waveforms: |  |  |  | time/div = |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & \mathrm{V}_{\mathrm{in}}=\quad \mathrm{V}_{\mathrm{p}-\mathrm{p}} \\ & \mathrm{~V}_{\mathrm{DC}, \mathrm{in}}=\ldots \end{aligned}$ |  |  |  |  | volts/div = |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |
| $\begin{aligned} & \mathrm{V}_{\text {out }}=\quad \mathrm{V}_{\mathrm{p}-\mathrm{p}} \\ & \mathrm{~V}_{\mathrm{DC}, \text { out }}=\ldots \end{aligned}$ |  |  |  |  | volts/div = |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |

TA's Signature: $\qquad$

| $\mathrm{C}=0.01 \mu \mathrm{~F}$ | Waveforms: |  |  | time/div = |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & \mathrm{V}_{\mathrm{in}}=\quad \mathrm{V}_{\mathrm{p}-\mathrm{p}} \\ & \mathrm{~V}_{\mathrm{DC}, \mathrm{in}}=\quad \end{aligned}$ |  |  |  |  | volts/div = |  |  |
|  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |
| $\begin{aligned} & \mathrm{V}_{\text {out }}=\quad \mathrm{V}_{\mathrm{p}-\mathrm{p}} \\ & \mathrm{~V}_{\mathrm{DC}, \text { out }}=\square \end{aligned}$ |  |  |  |  | volts/div = |  |  |
|  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |


| $\mathrm{C}=0.001 \mu \mathrm{~F}$ | Waveforms: |  |  |  | time/div = |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & \mathrm{V}_{\mathrm{in}}=\quad \mathrm{V}_{\mathrm{p}-\mathrm{p}} \\ & \mathrm{~V}_{\mathrm{DC}, \mathrm{in}}=\ldots \end{aligned}$ |  |  |  |  |  | volts/div $=$ |  |  |
|  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |
| $\begin{aligned} & \mathrm{V}_{\text {out }}=\quad \mathrm{V}_{\mathrm{p}-\mathrm{p}} \\ & \mathrm{~V}_{\mathrm{DC}, \text { out }}=\ldots \end{aligned}$ |  |  |  |  |  | volts/div $=$ |  |  |
|  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |

TA's Signature: $\qquad$

## QUESTIONS

1. Find the output $\mathrm{V}_{\mathrm{o}}(\mathrm{t})$ of the integrator shown in Fig. $\mathrm{Q}-1$ which responses to the input shown in Fig. Q-2. Assume $\mathrm{R}=10 \mathrm{k} \Omega, \mathrm{C}=10 \mathrm{nF}$ and $\mathrm{v}_{\mathrm{o}}(0)=0$.


Figure Q-1: An integrator


Figure Q-2: Step input
(a) - 10 t for $0 \leq \mathrm{t} \leq 1 \mathrm{~ms}$
(b) -100 t for $0 \leq \mathrm{t} \leq 1 \mathrm{~ms}$
(c) - 1000 t for $0 \leq \mathrm{t} \leq 1 \mathrm{~ms}$
(d) - 10000 t for $0 \leq \mathrm{t} \leq 1 \mathrm{~ms}$
(e) None of above.
2. If a $\qquad$ voltage is present at the input of the integrator op amp, the output voltage will be a
$\qquad$ slope output.
(a) negative, negative
(b) positive, positive
(c) negative, positive
(d) positive, zero
(e) None of above.
3. Consider an inverting integrator shown in Figure $\mathrm{Q}-1$. The input $v_{s}(t)$ is plotted in Figure Q-3. Suppose $\mathrm{v}_{\mathrm{o}}(0)=$ 0 and $T=R C$. Plot $\mathrm{v}_{\mathrm{o}}(\mathrm{t})$


Figure Q-3: Triangular Input

